Long-term volumetric eruption rates and magma budgets

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[1] A global compilation of 170 time-averaged volumetric volcanic output rates (Q_e) is evaluated in terms of composition and petrotectonic setting to advance the understanding of long-term rates of magma generation and eruption on Earth. Repose periods between successive eruptions at a given site and intrusive:extrusive ratios were compiled for selected volcanic centers where long-term (>10^4 years) data were available. More silicic compositions, rhyolites and andesites, have a more limited range of eruption rates than basalts. Even when high Q_e values contributed by flood basalts (9 ± 2 x 10^{-3} km^3/yr) are removed, there is a trend in decreasing average Q_e with lava composition from basaltic eruptions (2.6 ± 1.0 x 10^{-2} km^3/yr) to andesites (2.3 ± 0.8 x 10^{-3} km^3/yr) and rhyolites (4.0 ± 1.4 x 10^{-3} km^3/yr). This trend is also seen in the difference between oceanic and continental settings, as eruptions on oceanic crust tend to be predominately basaltic. All of the volcanoes occurring in oceanic settings fail to have statistically different mean Q_e and have an overall average of 2.8 ± 0.4 x 10^{-2} km^3/yr, excluding flood basalts. Likewise, all of the volcanoes on continental crust also fail to have statistically different mean Q_e and have an overall average of 4.4 ± 0.8 x 10^{-3} km^3/yr. Flood basalts also form a distinctive class with an average Q_e nearly two orders of magnitude higher than any other class. However, we have found no systematic evidence linking increased intrusive:extrusive ratios with lower volcanic rates. A simple heat balance analysis suggests that the preponderance of volcanic systems must be open magmatic systems with respect to heat and matter transport in order to maintain eruptible magma at shallow depth throughout the observed lifetime of the volcano. The empirical upper limit of ~10^{-2} km^3/yr for magma eruption rate in systems with relatively high intrusive:extrusive ratios may be a consequence of the fundamental parameters governing rates of melt generation (e.g., subsolidus isentropic decompression, hydration due to slab dehydration and heat transfer between underplated magma and the overlying crust) in the Earth.

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1. Introduction

 Despite the significant impact of volcanic systems on climate, geochronological cycles, geothermal resources and the evolution and heat budget of the crust, surprisingly little is known regarding the systematics of long-term rates of magma generation and eruption on Earth. Global rates of magma generation provide insight regarding the planetary-scale energy budget and thermal evolution of the Earth. Rates of magma generation and eruption are key factors affecting the petrological and geochemical evolution of magma bodies as well as eruptive styles due to the intrinsic coupling between magma recharge, fractional crystallization, wall rock assimilation and melt volatile saturation [Shaw, 1985; Spera et al., 1982]. Volcanoes and formation of intrusive bodies such as sill complexes have been suggested to play a role in global climate change [Svensen et al., 2004] and perhaps even trigger biotic extinctions. In addition, global rates of magmatism may have important implications for seismic energy release [Shaw, 1980] and the magnetic geodynamo by modulating heat transfer from the core-mantle boundary and the concomitant development of deep mantle plumes [Olson, 1994]. Rates of magmatism on Earth are also used in planetary research as analogues to constrain magmatic and thermal models. In summary, there is an exhaustive set of reasons for developing systematic knowledge regarding the rates of magmatism on Earth including the effects of magma composition and petrological environment on volumetric rates.

 One of the key factors in understanding magmatism is a quantitative evaluation of the extent to which magmatic systems operate as open or closed systems. These alternatives have significantly different implications for magma evolution. However, the openness of magmatic systems is difficult to determine since there is no unambiguous way to track magma transport from the generation and segregation through the crust to volcanic output. On balance, many magma systems are thought to be open systems in that they receive additional inputs of heat and mass during magmatic evolution [Davidson et al., 1988; Fowler et al., 2004; Gamble et al., 1999; Hildreth et al., 1986; Petford and Gallagher, 2001]. Closed magmatic systems which exchange heat but little material with their surroundings (i.e., neither assimilation nor recharge is important) may be rather uncommon. What is more likely is that specific systems may behave as closed systems for restricted portions of their history [e.g., Singer et al., 1992; Zielinski and Frey, 1970]. It is important to note, however, for the olivine basalt-trachyte series at Gough Island where fractional crystallization appears dominant, Pb and Sr isotopic data indicates that assimilation of hydrothermally altered country rock and/or recharge of isotopically distinct magma has taken place [Oversby and Gast, 1970].

 In this paper, time-averaged volcanic output for periods >10$^3$ years are evaluated. Volcanic output rates for individual eruptions may vary wildly about some norm, but evidently settle to a representative “average” value when time windows on the order of 10 times the average interval of eruptions are considered [Wadge, 1982]. Crisp [1984] conducted a similar study of magmatic rates published between 1962 and 1982 and established some basic relationships between volcanic output and associated factors such as crustal thickness, magma composition, and petrological setting. This work updates and extends that earlier compilation with 98 newly published volcanic rates and volumes from 1982–2004 for a total of 170 estimates (see auxiliary material$^1$ Tables S1 and S2). We also endeavor to establish some scaling relationships based primarily on the compilation and some simple energy budget considerations with the goal of discovering possible systematic trends in the data.

2. Sources and Quality of the Data

 The data presented here are volumetric volcanic or intrusive rates published from 1962–2005, including data from the compilation by Crisp [1984] of rates published from 1962–1982 where these data have not been superseded by more recent studies. We have also reviewed the rate data presented by Crisp [1984] and corrected or removed several references as appropriate. Thus the data presented here is a completely updated compilation of volumetric rates of eruption.

 Most volcanoes have cycles of intense activity followed by repose. Comparing volcanic systems at different stages in their eruptive cycles can lead to erroneous conclusions, if the duration of activity is not long enough to average the full range of eruptive behavior over the lifetime of the volcano. The duration needed depends upon the individual volcano; longer periods are generally required for

volcanic centers erupting more compositionally evolved magma due to lower eruption recurrence interval. Thus a period of ~10^3 years may be a long time for a basaltic shield volcano (e.g., Kilauea, Hawaii) but captures only an insignificant fraction of one eruptive cycle at a rhyolitic caldera (e.g., Yellowstone, USA). Only long-term rates are considered in this study although this reduces the available data considerably. We have culled the data to include primarily those estimates over 10^4 years or longer, but have selected a few volcanic centers with shorter durations where the shorter time interval did not compromise the data quality (e.g., capturing several eruptive cycles, smaller volcanic centers, or similar reasons) in our judgment.

Tables 1 and 2 show volcanic output rates for primarly mafic and silicic systems respectively. Output rates for volcanic systems (Q_o) are determined by dividing volcanic output volume by the duration of the activity. For longer durations activity may not have been continuous. By use of density for different compositions [Spera, 2000] we can convert volume rate (Q_o) to mass rate, which is probably the more fundamental parameter. Since density varies only slightly (basalt is ~15% denser than rhyolite at the same temperature and pressure) compared to the uncertainty in the data and the original data is all reported in terms of volume, we use Q_o exclusively in the rest of this study although mass rates are also given in Tables 1 and 2. Within each table, the rate estimates encompassing large areas, such as entire arcs or extensive volcanic fields, is presented separately from rates for individual volcanoes or smaller fields of vents. To remove ambiguity from the decision, a cutoff of 10^4 km^2 was used to separate global data sets, typically involving compilations of several volcanoes themselves, from local data sets focused on individual volcanoes with a more constrained study area. However, we find that rates for entire arcs/fields when presented as km^3/yr per 100 km are similar to those for individual volcanoes (Figure 1).

A large amount of uncertainty is associated with inferring volcanic rates from unobserved eruptions. In the tables, a “Notes” field contains information about the methods used to derive the estimates and uncertainties that were available in the original literature, but in many cases no formal uncertainties were reported. Generally the rates reported here should be taken as order-of-magnitude estimates although in some cases the uncertainties may be as small as a factor of two. The extrusive rate often depends on the duration considered; therefore data for one volcanic center measured over different durations are included in Tables 1 and 2. The period of volcanism may also be important since eruptions from further in the past may have experienced more erosion, partial burial, or be more difficult to accurately date.

Sources of error reported in the original publications, as well as most unquantified unreported error, mainly arise from estimating (1) the thickness of the volcanic deposits, (2) the age of lavas, or (3) amount of erosion. Less significant potential sources of error are uncertainty in the conversion from volume to dense rock equivalent (DRE) volume, and uncertainty in the area covered by deposits. One may attribute some of the variance in rates to error introduced by comparing volcanic systems at different scales. For example, the volcanic output rate over continuous lengths of oceanic arcs and ridges is expected to be higher than small individual volcanoes. The arcs and ridges are divided into unit volcano lengths of 100 km based on the spacing of volcanoes in arcs [de Bremond d’Ars et al., 1995]. Petrologic and tectonic factors are also reported for each volcanic system where data are available include lithic type or bulk wt% SiO_2 of erupted magma, and petrotectonic setting. Rock names are given for the dominant magma type associated with each area simplified in one of the following categories: basalt, basaltic andesite, andesite, rhyolite. The mode wt% SiO_2 reported here is the mode of erupted products by volume reported within the given period for that volcanic system. Petrologic setting groups the systems into six categories based on crustal type, oceanic or continental, and association with a plate boundary type; convergent, divergent, or intraplate.

3. Volcanic Rates and Regimes

3.1. Rates of Eruption

Eruption rates are examined on the basis of dominant lithology and petrotectonic setting. Rock type affects many factors related to flow behavior such as viscosity, temperature, and pre-eruptive volatile content. Thus it may be an important control on eruption rate. Petrologic setting most strongly reflects the magma generation process, but is also a way to qualitatively look at the effects of crustal thickness.

The effect of magma composition on eruption rate is assessed by broadly grouping the lavas from a volcanic area into one of four categories based on the dominant SiO_2 of the reported rock composi-
Table 1 (Representative Sample). Rates and Volumes of Basaltic Volcanism [The full Table 1 is available in the HTML version of this article at http://www.g-cubed.org]

<table>
<thead>
<tr>
<th>Location (Volcano Name)</th>
<th>Duration, Myr</th>
<th>Extrusive Volume, km$^3$</th>
<th>Volume Extrusion Rate, Q, km$^3$ yr$^{-1}$</th>
<th>Mass Extrusion Rate, kg yr$^{-1}$</th>
<th>Bulk SiO$_2$</th>
<th>Petrotextonic Setting</th>
<th>Notes</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ascension</td>
<td>1.500</td>
<td>90</td>
<td>6.00E−05</td>
<td>1.49E+09</td>
<td>48</td>
<td>oceanic hot spot</td>
<td>Rough estimate of volumes from topography; rates constrained by a few K-Ar dates since 1.5 Ma.</td>
<td>Gerlach [1990], Nielson and Sibbett [1996]</td>
</tr>
<tr>
<td>Auckland, New Zealand</td>
<td>0.140</td>
<td>2</td>
<td>1.07E−05</td>
<td>2.89E+07</td>
<td>B</td>
<td>Continental volcanic field</td>
<td>Volume calculated from thickness and areal extent based on field mapping and boreholes for 49 volcanic centers and adjusted to DRE volume. Active for last 140 kyr based on K-Ar, thermoluminescence, and $^{14}$C dates.</td>
<td>Allen and Smith [1994]</td>
</tr>
<tr>
<td>Bouvet</td>
<td>0.700</td>
<td>28</td>
<td>4.00E−05</td>
<td>4.59E+08</td>
<td>48</td>
<td>oceanic hot spot</td>
<td>Very rough estimate of volume from island topography; active for the past 0.7 Myr.</td>
<td>Gerlach [1990]</td>
</tr>
<tr>
<td>Camargo, Mexico</td>
<td>4.64</td>
<td>120</td>
<td>2.6E−05</td>
<td>7.02E+07</td>
<td>B</td>
<td>Continental volcanic field</td>
<td>Constraints from K-Ar dates from 4.73 ± 0.04 Ma to 0.09 ± 0.04 Ma. Volume based on an area of 3000 km$^2$ and average thickness of 40 m</td>
<td>Aranda-Gomez et al. [2003]</td>
</tr>
<tr>
<td>La Palma, Canary Islands</td>
<td>0.123</td>
<td>125</td>
<td>1.0E−03</td>
<td>2.70E+09</td>
<td>48</td>
<td>oceanic hot spot</td>
<td>Detailed field observations, mapping, and $^{39}$Ar/$^{40}$Ar dating of uneroded Cumbre Viejo indicate activity since 123 ± 3 ka.</td>
<td>Carracedo et al. [1999], Guillou et al. [1998]</td>
</tr>
<tr>
<td>Santo Antao, Cape Verdes</td>
<td>1.750</td>
<td>68</td>
<td>4.00E−05</td>
<td>1.08E+08</td>
<td>48</td>
<td>oceanic hot spot</td>
<td>Rates from main shield-building stage Cha de Morte volcanics deposited between 2.93 ± 0.03 and 1.18 ± 0.01 Ma ($^{39}$Ar/$^{40}$Ar ages) and field mapping.</td>
<td>Plesner et al. [2002]</td>
</tr>
<tr>
<td>Coso, CA</td>
<td>1.500</td>
<td>24.3</td>
<td>1.60E−05</td>
<td>5.40E+12</td>
<td>57</td>
<td>continental volcanic field</td>
<td>Field mapping estimate of 23–25.5 km$^3$ erupted between 4.02 ± 0.06 and 2.52 ± 0.05 Ma (K-Ar ages).</td>
<td>Duffield et al. [1980]</td>
</tr>
<tr>
<td>Location</td>
<td>Duration, Myr</td>
<td>Extrusive Volume, km³</td>
<td>Volume Extrusion Rate, Q, km³ yr⁻¹</td>
<td>Mass Extrusion Rate, kg yr⁻¹</td>
<td>SiO₂ Wt%</td>
<td>Petrotectonic Setting</td>
<td>Notes</td>
<td>References</td>
</tr>
<tr>
<td>--------------------------</td>
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<td>-----------------------------------------------------------------------</td>
<td>-------------------------------------</td>
</tr>
<tr>
<td>Alban Hills, Italy</td>
<td>0.561</td>
<td>290</td>
<td>5.2E⁻⁰⁴</td>
<td>1.33E⁺⁰⁹</td>
<td>A</td>
<td>Continental arc</td>
<td>Geologic map. Some ages from thermoluminescence. Period of eruptions 580 ka to 19 ka. Not corrected for DRE. Unknown amount of erosion.</td>
<td>Chiarebba et al. [1997]</td>
</tr>
<tr>
<td>Asama</td>
<td>0.030</td>
<td>37</td>
<td>1.20E⁻⁰³</td>
<td>8.61E⁺⁰⁸</td>
<td>A</td>
<td>oceanic arc</td>
<td>37 ± 7 km³ erupted over past 0.03 Myr</td>
<td>Crisp [1984]</td>
</tr>
<tr>
<td>Avachinsky, USSR</td>
<td>0.060</td>
<td>100</td>
<td>1.70E⁻⁰⁵</td>
<td>1.62E⁺⁰⁸</td>
<td>BA</td>
<td>continental arc</td>
<td>Rough estimate excluding ejecta beyond cone.</td>
<td>Crisp [1984]</td>
</tr>
<tr>
<td>Ceboruco-San Pedro</td>
<td>0.8</td>
<td>80.5</td>
<td>8.05E⁻⁰⁵</td>
<td>2.05E⁺⁰⁸</td>
<td>A</td>
<td>continental arc</td>
<td>Volume determinations 80.5 ± 3.5 km³ from field mapping, digital topography, and orthophotos. Only minor erosion. Age from numerous ⁴⁰Ar/³⁹Ar dates.</td>
<td>Frey et al. [2004]</td>
</tr>
<tr>
<td>Ceboruco-San Pedro</td>
<td>0.1</td>
<td>60.4</td>
<td>6.04E⁻⁰⁴</td>
<td>1.54E⁺⁰⁹</td>
<td>A</td>
<td>continental arc</td>
<td>Volume determinations from field mapping, digital topography, and orthophotos. Only minor erosion. Age from numerous ⁴⁰Ar/³⁹Ar dates.</td>
<td>Frey et al. [2004]</td>
</tr>
<tr>
<td>Clear Lake, California</td>
<td>2.050</td>
<td>73</td>
<td>3.50E⁻⁰⁵</td>
<td>2.81E⁺⁰⁹</td>
<td>64</td>
<td>Continental Volcanic Field</td>
<td>For period from 2.06–0.01 Ma. Volume includes estimate of eroded material.</td>
<td>Crisp [1984]</td>
</tr>
<tr>
<td>Coso, California</td>
<td>0.4</td>
<td>2.4</td>
<td>5.7E⁻⁰⁶</td>
<td>1.34E⁺⁰⁷</td>
<td>R</td>
<td>Continental Volcanic Field</td>
<td>Geologic mapping estimate of 0.9 km³ of basalt and 1.5 km³ of rhyolite erupted over past 0.4 Myr based on K-Ar ages.</td>
<td>Bacon [1982]</td>
</tr>
<tr>
<td>Davis Mountains, Texas</td>
<td>1.5</td>
<td>1525</td>
<td>1.0E⁻⁰³</td>
<td>2.35E⁺⁰⁹</td>
<td>R</td>
<td>Continental Volcanic Field</td>
<td>Detailed field mapping and ⁴⁰Ar/³⁹Ar Ar ages from 36.8 to 35.3 Ma. No DRE correction applied, as deposits have low porosity. The actual total volume may be as high as 2135 km³, if buried lava flows over full extent of area suggested.</td>
<td>Henry et al. [1994]</td>
</tr>
<tr>
<td>Fuji</td>
<td>0.011</td>
<td>88</td>
<td>8.00E⁻⁰³</td>
<td>4.59E⁺⁰⁸</td>
<td>BA</td>
<td>oceanic arc</td>
<td>Volume estimated from detailed field mapping for eruptions over past 11 kyr (tephrachronology)</td>
<td>Togashi et al. [1991]</td>
</tr>
</tbody>
</table>
White et al.: Eruption rates and magma budgets

Volcanic systems can be classified into categories based on rock type and petrotectonic setting. Among the major rock type groups we have used here, the mean and variance of \( Q_e \) decreases as the amount of silica increases. In Figure 1, this trend is apparent as the basalts form a wide field of values whose mean is \( 10^{-2} \) km\(^3\)/yr while andesites and rhyolites form a much narrower band of values around \( 10^{-3} \) km\(^3\)/yr. The flood basalts form a small cluster of values above 1 km\(^3\)/yr on Figure 1, outside of a more uniform field of values for all compositions, and seem to form a distinct group. Therefore flood basalts were not considered with the rest of the basalt rates when comparing to other compositions to avoid skewing the results. With flood basalts removed, basaltic eruptions still have an order-of-magnitude higher average rate (2.6 ± 1.0 \( \times \) 10\(^{-2} \) km\(^3\)/yr) than basaltic andesites, andesites and rhyolites. Average rates for andesites (2.3 ± 0.8 \( \times \) 10\(^{-3} \) km\(^3\)/yr) and rhyolites (4.0 ± 1.4 \( \times \) 10\(^{-3} \) km\(^3\)/yr) are also significantly different, although not as distinct as the difference between basalts and these two groups.

The effect of petrotectonic setting on eruption rate is assessed by grouping the volcanoes by the main differences in magma genesis based on plate tectonic theory. In contrast to lithology, petrotectonic setting lends itself to grouping into categories (Figure 2). Volcanoes at convergent plate boundaries are arcs, divergent plate boundaries are rifts or spreading ridges, and intraplate volcanoes are so-called hot spots. Also included is a separate designation of volcanic fields (continental volcanic fields) for areas characterized by areally distributed volcanism of primarily small (<1 km\(^3\)), monogenetic cones. These fields tend to occur in regions that are difficult to classify by traditional plate tectonic theory such as slab windows (e.g., Clear Lake, CA) or continental extension (e.g., Lunar Crater, NV). In order to also assess the role of crustal thickness/composition, the petrotectonic settings are further subdivided into volcanoes erupting through continental or oceanic crust. The exceptions are oceanic plateaux, the flood basalt equivalent for oceanic crust. Reliable data are so sparse for plateaux that we have grouped oceanic and continental flood basalts in Figure 2.

Basalts exhibit a wider range of eruption rates than other rock types, ranging from <10\(^{-5} \) km\(^3\)/yr to >1 km\(^3\)/yr (Figure 1). Basaltic systems in general show both short-term and long-term changes in eruption rates especially in long-lived systems (e.g., Hawaii [Dvorak and Dzurisin, 1993; Vidal and Bonneville, 2004]). More-silicic rock types, the rhyolites and andesites, have a more limited range of eruption rates than basalts. Long-term rates for silicic eruptions range from <10\(^{-5} \) km\(^3\)/kyr to 10\(^{-2} \) km\(^3\)/yr (Table 2 and Figure 1).

Figure 1. Volumes and volcanism durations for locations in Tables 1 and 2 (see also auxiliary material Tables S1 and S2). The diagonal lines represent constant rates of volcanic output. The points are coded by color and shape to indicate lava composition by SiO\(_2\) content. Open symbols represent rates for arc and large areas (>10\(^4 \) km\(^2\)), and solid symbols represent individual volcanoes and small volcanic fields (<10\(^4 \) km\(^2\)).
A very wide range of eruption rates have been reported for oceanic hot spots that overlap significantly with oceanic arcs and ocean spreading ridges. Although the mean $Q_e$ appears higher for oceanic hot spots than other classes of oceanic volcanism, the two-tailed $t$-test indicates that $Q_e$ for all groups of oceanic volcanism are not statistically different. When grouped by petro-tectonic setting, $Q_e$ from continental areas tend to be lower on average than for oceanic areas, however the range of output rates for any one setting overlaps all other settings (Figure 2).

Crisp [1984] noted a similar pattern of higher eruption rates in oceanic settings although found no specific value of crustal thickness that acted as a filter threshold. All of the volcanoes occurring in oceanic settings fail to have statistically different mean $Q_e$ and have an overall average of $2.8 \pm 0.5 \times 10^{-2}$ km$^3$/yr. Likewise, all of the volcanoes on continental crust also fail to have statistically different mean $Q_e$ and have an overall average of $4.4 \pm 0.8 \times 10^{-3}$ km$^3$/yr, excluding flood basalts. A two-tailed $t$-test for means indicates that oceanic and continental $Q_e$ are statistically different. This implies that crustal thickness, as the overarching contrast between oceanic and continental lithosphere, exerts some control on volcanic rates. Flood basalts also form a distinctive class of volcanism with an average $Q_e$ ($9 \pm 2 \times 10^{-1}$ km$^3$/yr) two orders of magnitude larger than the range of any other class (Figure 2).

### 3.2. Intrusive:Extrusive Ratios

The average and range of intrusive:extrusive (I:E) volume ratios for different petro-tectonic settings are useful in estimating hidden intrusive volumes at other locations and perhaps on other planets [Greeley and Schneid, 1991]. However, I:E ratios are difficult to estimate and rarely published because the plutonic rocks are either buried or the volcanic rocks are eroded, or the relationship between the volcanic and plutonic rocks is uncertain. Seismic, geodetic, and electromagnetic techniques can reveal the dimensions of molten or partially molten regions under a volcano. Likewise, the sulfur output by magma degassing can be used to estimate the volume of the cooling magma [Allard, 1997]. However, the size of the molten magma reservoir at one time in a longer history may not be a good indicator of the total intrusive volume. Likewise, broad constraints on intrusive volume based on petrologic modeling of the fractional crystallization of a parent basalt are not considered because they will always calculate lower bound on intrusive volume, because such calculations based on extrusive rocks cannot account for strictly intrusive events. Better estimates of total intrusive volume can sometimes be obtained by seismic or gravity measurements of buried plutons. Another way to determine I:E ratios is to compare geographically related volcanic and plutonic sequences. Three such determinations were made in this compilation for the Andes, the Bushveld Complex, and the Challis Volcanic Field-Casto Pluton. However, in each of these cases it is uncertain how well linked extrusive and intrusive rocks are in fact. Despite this uncertainty, we proceed with an analysis if for no other reason than to highlight that this issue has received so little attention.

Previous studies have reported a wide range of I:E ratios from 1:1 to 16:1 [Crisp, 1984; Shaw et al., 1980; Wadge, 1980]. Shaw [1980] hypothesized that the I:E ratio would be higher where crustal thickness is greater, up to 10:1. This makes sense since magma traveling greater path lengths through thicker continental crust has longer to cool...
### Table 3. Intrusive:Extrusive Ratios

<table>
<thead>
<tr>
<th>Volcano</th>
<th>Intrusive</th>
<th>Extrusive</th>
<th>Ratio</th>
<th>Method</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aleutians</td>
<td>1073–1738 km³/km</td>
<td>627–985 km³/km</td>
<td>1:1–3:1</td>
<td>Seismic and crystallization of Hidden Bay Pluton and related extrusives</td>
<td>Kay andKay [1985]</td>
</tr>
<tr>
<td>Bushveld-Rooiberg, South Africa</td>
<td>$1 \times 10^6$ km³</td>
<td>$3 \times 10^5$ km³</td>
<td>3:1</td>
<td>Stratigraphic mapping. Cr and incompatible trace element analyses indicate that the total magma volume intruded was approximately $1 \times 10^5$ km³.</td>
<td>Cawthorn and Walraven [1998], Schweitzer et al. [1997], Twist and French [1983]</td>
</tr>
<tr>
<td>Central Andes, Peru</td>
<td>$9–29 \times 10^4$ km³</td>
<td>$2.25 \times 10^4$ km³</td>
<td>3:1–12:1</td>
<td>Extrusive from geologic mapping.</td>
<td>Francis and Hawkesworth [1994], Haederle and Atherton [2002] Criss et al. [1984]</td>
</tr>
<tr>
<td>Challis Volcanic Field, Idaho</td>
<td>$3.5 \times 10^3$ km³</td>
<td>$4 \times 10^3 – 2.8 \times 10^4$ km³</td>
<td>&gt;1:1–8:1</td>
<td>Very uncertain; field and stratigraphic mapping; extrusive converted to DRE using 75% porosity; total plutonic thickness unknown.</td>
<td>Francis and Hawkesworth [1994], Haederle and Atherton [2002] Criss et al. [1984]</td>
</tr>
<tr>
<td>Coso Volcanic field, California</td>
<td>$2.8 \text{ km}^3/\text{Myr (basalt)}$</td>
<td>$570 \text{ km}^3/\text{Myr}$</td>
<td>1:200$^a$ 1:100$^a$</td>
<td>Extrusive from geologic mapping for the past 0.4 Myr; intrusive rate based on current heat flow and estimates of local tectonic extension.</td>
<td>Bacon [1983]</td>
</tr>
<tr>
<td>East Pacific Rise</td>
<td>7 km</td>
<td>0.5–0.8 km</td>
<td>5:1–8:1</td>
<td>Seismic; stratigraphic mapping.</td>
<td>Detrick et al. [1993], Harding et al. [1993], Karson [2002], Allard [1997], Hirn et al. [1991]</td>
</tr>
<tr>
<td>Etna, Italy (1 Ma)</td>
<td>$3 \times 10^2$ km³</td>
<td>$1 \times 10^2$ km³</td>
<td>3:1</td>
<td>Seismic (estimate for $\sim 0.1$ Ma).</td>
<td>Francis and Hawkesworth [1994], Haederle and Atherton [2002] Criss et al. [1984]</td>
</tr>
<tr>
<td>Italy (since 1975)</td>
<td>0.6 km³</td>
<td>5.9 km³</td>
<td>10:1</td>
<td>SO$_2$ flux 1975–1995 AD.</td>
<td>Bargar and Jackson [1974], Vidal and Bonneville [2004]</td>
</tr>
<tr>
<td>Hawaiian-Emperor Seamount Chain</td>
<td>$5.9 \times 10^6$ km³</td>
<td>$1.1 \times 10^6$ km³</td>
<td>6:1$^a$</td>
<td>Extrusive from topographic maps; intrusive from magmatic models and averaged over the past 74 Myr.</td>
<td>Bargar and Jackson [1974], Vidal and Bonneville [2004]</td>
</tr>
<tr>
<td>Kerguelen Archipelago</td>
<td>$9.9 \times 10^4$ km³</td>
<td>$2.75 \times 10^4$ km³</td>
<td>28:1$^a$</td>
<td>Seismic.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Kiluaea, Hawaii</td>
<td>$9 \times 10^2$ km³/yr</td>
<td>$5 \times 10^2$ km³/yr</td>
<td>2:1</td>
<td>Drill hole stratigraphy; ground deformation; geologic mapping.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Long Valley, California</td>
<td>$7.6 \times 10^3$ km³</td>
<td>$7.5 \times 10^3$ km³</td>
<td>10:1</td>
<td>Rough estimate from seismic tomography, stratigraphic mapping, drill holes, and gravity.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Marquesas Islands</td>
<td>$6.2 \times 10^5$ km³</td>
<td>$3.3 \times 10^5$ km³</td>
<td>2:1$^a$</td>
<td>Seismic.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Mauna Loa, Hawaii</td>
<td>$8 \times 10^3$ km³</td>
<td>$1.1–2.4 \times 10^3$ km³</td>
<td>&gt;1:1–3:1</td>
<td>Stratigraphic mapping, for the 1877–1950 time period.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Mid-Atlantic Ridge</td>
<td>5.5–7 km</td>
<td>0.5–1.5 km</td>
<td>5:1–10:1</td>
<td>Seismic.</td>
<td>Nicolaysen et al. [2000] Dvorak and Doraisin [1993], Quane et al. [2000], Hildreth [2004], McConnell et al. [1995], Weiland et al. [1995], Caress et al. [1995], Klein [1982], Lipman [1995]</td>
</tr>
<tr>
<td>Miyake, Japan</td>
<td>$4 \text{ km}^3$</td>
<td>$1.5 \times 10^3$ km³</td>
<td>3:1</td>
<td>Geodetic modeling; SO$_2$ emissions.</td>
<td>Kumagai et al. [2001] Walker [1993]</td>
</tr>
<tr>
<td>Mull Volcano, Scotland</td>
<td>$1.3 \times 10^4$ km³</td>
<td>$7.6 \times 10^3$ km³</td>
<td>2:1</td>
<td>Stratigraphic mapping.</td>
<td>Grevenmeyer et al. [2001], Nicolaysen et al. [2000]</td>
</tr>
</tbody>
</table>
and dissipate energy. In addition, mean crustal densities are closer to typical magma densities compared to the mantle (i.e., positive buoyancy forces are likely smaller for magma in the crust compared to magma in the mantle). Subsequently, Wadge [1982] made the argument based on steady state volcanic rates and indirect calculations of intrusive volume that less evolved systems have I:E ratios as low as 1:1.5 for basaltic shields on oceanic crust and up to 1:10 for rhyolite calderas on continental crust. Crisp [1984] presented 14 ratios but did not find any strong connection between magma composition and I:E ratio.

The I:E ratios in this compilation encompass a wide range of values but fails to show any systematic variations with eruptive style, volcanic setting, or total volume (Table 3). While some well-known basaltic shields do have I:E ratios of 1:1 to 2:1, the oceanic ridges have considerably higher ratios of at least 5:1. The range of estimates goes as high as 34:1 at Mount Pinatubo, and 200:1 for the Coso Volcanic Field. Conversely, the I:E ratios at calderas may be much lower than 10:1. Yellowstone has a fairly well constrained I:E ratio of 3:1. Continental magma systems that have had detailed geophysical investigations tend to have magma chamber volume estimates comparable to the total erupted volume, as noted by Marsh [1989]. A ratio of 5:1 could be viewed as common to most magmatic systems when the considerable uncertainty is considered. Ratios higher than 10:1 are uncommon in our data set. When volume of magma involved in crustal “underplating” or magmatic addition to the lower crust is also counted, much higher ratios of intrusive:extrusive activity sometimes result (Ninetyeast Ridge [Frey et al., 2000], Coso [Bacon, 1983]) but other times do not (Aleutians [Kay and Kay, 1985], Marquesas [Caress et al., 1995]).

### 3.3. Repose Time Between Volcanic Events

A major discriminant in the behavior of volcanic systems is their frequency of eruptions through time. Most basaltic volcanoes erupt small volumes of lava frequently whereas continental calderas erupt great volumes of silicic magma infrequently. At Hekla, Thorarinsson and Sigvaldason [1972] noted a positive relationship between repose length and the silica content of the initial lavas erupted following the repose. Data from 17 volcanic centers in Table 4 selected to span a wide range of SiO₂ content define an exponential relationship between repose time and SiO₂ content in the lava (Figure 3). The volcanic centers in Table 4 were chosen to span
a range of SiO$_2$ compositions for sequences of at least three eruptions.

[19] The minimum, maximum, and mean repose time for an eruption sequence is presented along with the minimum and maximum SiO$_2$ content for the corresponding suite of compositions erupted from a “single” center. Repose time is determined by the interval between the end of one eruption and the start of the next. Measuring repose time is somewhat subjective because what may count as a repose at one volcano may not be considered as a repose elsewhere. Closely observed volcanoes (e.g., Etna or Kilauea) have reposes reported on a scale of days but on older or more silicic volcanoes (e.g., Santorini or St. Helens) have their eruptive periods divided into major eruptive units separated by thousands of years. We have tried to determine repose period as the length of time between eruptions of a characteristic size for that volcano. For example, at Santorini reposes between the Kameni dome-forming eruptions are much shorter than the major ashfall eruptions [Druitt et al., 1999]. This example also highlights the potential for bias

### Table 4. Repose Times at Selected Volcanic Centers

<table>
<thead>
<tr>
<th>Volcano</th>
<th>Repose Time</th>
<th>Repose Min, years</th>
<th>Repose Max, years</th>
<th>Number of Reposes in Record</th>
<th>wt% SiO$_2$ min</th>
<th>wt% SiO$_2$ max</th>
<th>References</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>Colima</td>
<td>80</td>
<td>48</td>
<td>138</td>
<td>3</td>
<td>56</td>
<td>61</td>
<td>Luhr and Carmichael [1980]</td>
<td>Four cycles of activity ending with ash flow eruptions since 1576 AD.</td>
</tr>
<tr>
<td>Etna</td>
<td>4</td>
<td>0.1</td>
<td>100</td>
<td>70</td>
<td>47</td>
<td>50</td>
<td>Tanguy [1979], Wadge [1977]</td>
<td>Constrained by historical records from 1536 to 2001 AD.</td>
</tr>
<tr>
<td>Fogo, Cape Verde</td>
<td>20</td>
<td>1</td>
<td>94</td>
<td>27</td>
<td>40</td>
<td>42</td>
<td>Doucelance et al. [2003], Trustell et al. [1995]</td>
<td>Constrained by historical records from 1500 to 1995 AD.</td>
</tr>
<tr>
<td>Fuego</td>
<td>100</td>
<td>10</td>
<td>150</td>
<td>60</td>
<td>49</td>
<td>55</td>
<td>Martin and Rose [1981]</td>
<td>Constrained by historical records since 1500 AD; eruptions occur in clusters of activity.</td>
</tr>
<tr>
<td>Izu-Oshima</td>
<td>68</td>
<td>13</td>
<td>190</td>
<td>23</td>
<td>53</td>
<td>57</td>
<td>Koyama and Hayakawa [1996]</td>
<td>Detailed syncaic and postcaldera eruptive history from tephra and loess stratigraphy; reposes since caldera formation.</td>
</tr>
<tr>
<td>Katla</td>
<td>46</td>
<td>13</td>
<td>80</td>
<td>20</td>
<td>46</td>
<td>50</td>
<td>Larsen [2000]</td>
<td>Last 11 centuries; constrained by historical records.</td>
</tr>
<tr>
<td>Kilauea</td>
<td>0.8</td>
<td>0.1</td>
<td>10</td>
<td>46</td>
<td>48</td>
<td>50</td>
<td>Klein [1982]</td>
<td>Constrained by historical records from 1918 to 1979 AD.</td>
</tr>
<tr>
<td>Mauna Loa</td>
<td>5</td>
<td>0.1</td>
<td>20</td>
<td>34</td>
<td>48</td>
<td>50</td>
<td>Klein [1982]</td>
<td>Constrained by historical records from 1843 to 1984 AD.</td>
</tr>
<tr>
<td>Mt Adams</td>
<td>150000</td>
<td>500000</td>
<td>320000</td>
<td>3</td>
<td>57</td>
<td>64</td>
<td>Hildreth and Fierstein [1997], Hildreth and Lanphere [1994]</td>
<td>Major cone building episodes since 500 ka.</td>
</tr>
<tr>
<td>Mt St Helens</td>
<td>8600</td>
<td>50000</td>
<td>150000</td>
<td>6</td>
<td>63</td>
<td>67</td>
<td>Doukas [1990], Mullineaux [1996]</td>
<td>From 40 ka to present, major eruptive cycles only. Constrained by $^{40}$Ar/$^{39}$Ar ages.</td>
</tr>
<tr>
<td>Ruapehu</td>
<td>30000</td>
<td>100000</td>
<td>600000</td>
<td>5</td>
<td>55</td>
<td>65</td>
<td>Gamble et al. [2003]</td>
<td>For major explosive volcanism since 360 ka. Both $^{40}$Ar/$^{39}$Ar and K-Ar ages for older units, radiocarbon ages for younger.</td>
</tr>
<tr>
<td>Santorini</td>
<td>30000</td>
<td>170000</td>
<td>400000</td>
<td>12</td>
<td>58</td>
<td>71</td>
<td>Druitt et al. [1999]</td>
<td></td>
</tr>
<tr>
<td>Taupo</td>
<td>2000</td>
<td>20</td>
<td>6000</td>
<td>28</td>
<td>72</td>
<td>76</td>
<td>Sutton et al. [2000]</td>
<td>Post-Oruanui eruptions from 26.5 ka to present.</td>
</tr>
<tr>
<td>Toba</td>
<td>375000</td>
<td>340000</td>
<td>430000</td>
<td>3</td>
<td>68</td>
<td>77</td>
<td>Chesner and Rose [1991]</td>
<td>Reposes between tuff-forming eruptions since 0.8 Ma.</td>
</tr>
<tr>
<td>Valles</td>
<td>335000</td>
<td>320000</td>
<td>350000</td>
<td>3</td>
<td>69</td>
<td>75</td>
<td>Doell et al. [1968], Heiken et al. [1990]</td>
<td>Reposes based on eruption of Bandelier and pre-Bandelier tuff, and collapse of Toledo and Valles calderas.</td>
</tr>
<tr>
<td>Yatsugatake</td>
<td>32000</td>
<td>10000</td>
<td>85000</td>
<td>5</td>
<td>53</td>
<td>63</td>
<td>Kaneoka et al. [1980], Oishi and Suzuki [2004]</td>
<td>Plinian eruptions since 0.2 Ma. Tephrochronology and radiocarbon ages.</td>
</tr>
<tr>
<td>Yellowstone</td>
<td>700000</td>
<td>600000</td>
<td>800000</td>
<td>3</td>
<td>75</td>
<td>79</td>
<td>Christiansen [2001]</td>
<td>Considers major tuff-forming eruptions.</td>
</tr>
</tbody>
</table>
toward the Recent with shorter repose times for smaller eruptions that are not preserved in the long-term geologic record. For these reasons, the repose periods between major eruptions are considered whereas the “leaking” of minor volumes of lava between major eruptions is not considered in this study.

The exponential relationship between SiO$_2$ content and repose time is mainly determined by basaltic shields and rhyolite calderas. For volcanoes in the andesite-dacite range, the data jump from short repose intervals to longer repose at ~60% SiO$_2$ (Figure 3). While composition is unlikely to be the exclusive control on repose time, more error is likely to emerge in the 60–70% SiO$_2$ range due to difficulties in dating the eruptions of complex stratocones, the dominant constructional volcanic morphology for intermediate compositions. Measuring the repose periods at stratocones and calderas requires high resolution stratigraphy and precise ages over several millennia to smooth out the short-timescale volume/frequency relationship [Wadge, 1982]. These data are very limited but are becoming more available recently with improvements in geochronological methods [Hildreth et al., 2003a]. If the maximum SiO$_2$ in the system controls the repose period then the fit parameter of the exponential equation improves slightly ($R^2 = 0.69$ to 0.73).

There are several reasons to expect repose time to increase as silica increases. Direct melting of mantle produces basaltic compositions, and more evolved compositions require time for fractional crystallization and assimilation. Higher silica compositions also have greater melt viscosity, requiring additional excess pressure to erupt [Rubin, 1995] and, in that sense, are far less mobile. More viscous magmas are more likely to suffer “thermal death” compared to less viscous magmas. A few studies have already pointed out a positive correlation between eruptive volume and repose interval [Cary et al., 1995; Klein, 1982; Wadge, 1982]. The magma storage time, based on rock geochronometers from crystal ages and from crystal size distribution analysis (CSD), tends to increase exponentially as SiO$_2$ and stored magma volume increase [Hawkesworth et al., 2004; Reid, 2003]. These observations are all consistent with the idea that longer magma storage times allow time for that, in turn, results in longer repose periods associated with higher silica content magmas.

4. Discussion

4.1. Upwelling and Magma Production Rate Limits

Factors that might influence volcanic rates and intrusive:extrusive ratios are local crustal thickness, tectonic setting (magnitude and orientation of principal stresses), magma composition, and melt generation rate in the source region. For 170 examples, long-term volcanic output rate varies...
from $10^{-5}$ to 1 km$^3$/yr. Only flood basalts attain the highest $Q_e$, above $10^{-1}$ km$^3$/yr, while various volcanoes with the lowest measured $Q_e$, below $10^{-5}$ km$^3$/yr, seem to have very little in common (Figure 1). Tectonic setting, but not magma composition, affects volcanic rates. Continental crust reduces the average $Q_e$ to $4.4 \times 10^{-3}$ km$^3$/yr from $2.8 \times 10^{-2}$ for oceanic crust.

The output rates all show a strong skewness with long tails toward low $Q_e$ values suggesting that an upper limit may exist (Figure 2). Furthermore, although there is essentially no lower limit to volcanic rates in that magma supplied from depth may intrude but never erupt, or dribble out slowly, this is not usually the case. Most volcanoes have a $Q_e$ above $1 \times 10^{-3}$ km$^3$/yr. This result was also found empirically by Smith [1979] and Crisp [1984]. Hardee [1982] derives a simple analytic solution showing that this critical $Q_e$ of $10^{-3}$ km$^3$/yr represents a “thermal threshold” where magmatic heat from the intrusion tends to keep a conduit open and begin formation of a magma chamber. We infer that long-term volcanism is unlikely to occur without an open magma conduit to supply and focused melt delivery. This threshold value is dependent on intrusive rate, not volcanic output rate. The I:E ratios found are somewhat lower than the often cited 10:1 ratio, and suggest that an I:E ratio of $\sim$5:1 may be regarded as a better average value. Nevertheless, this suggests that, using the $Q_e$ values present here as data for the Hardee [1982] model, virtually all of the volcanic systems in Tables 1 and 2 meet the requirements for conduit wall rock meltback and magma chamber formation.

It is perhaps surprising that given the large differences in eruptive style and melt generation mechanisms (e.g., isentropic decompression, triggering by metasomatic introduction of volatiles or mafic magma underplating) in different tectonic settings an aggregate view of volcanic rates exhibits such a small range of variation, by and large. The similarity of the rates leads us to speculate that a magma upwelling rate limit is set within the mantle at a value near 1 km$^3$/yr, with magma generation being subject to greater variances based on the local composition of the mantle being melted. In this view, flood basalts represent systems with low I:E ratios and form when a large fraction of mantle-generated magma reaches the surface. The upper limit on magma generation may be controlled by the subsolidus upwelling rate within the upper mantle of 0.01–0.1 m/yr, and this may explain the upper limit of magma generation due to isentropic decompression [Asimow, 2002; Verhoogen, 1954].

4.2. Openness of Magmatic Systems

The volcanic output rate and repose periods between eruptions gives us some basic constraints on the behavior of magma systems as open or closed systems. We have noted the empirical correlation of repose period and magma silica content. That is, a repose interval can be roughly predicted on the basis of either mean or maximum SiO$_2$ wt% of the eruptive composition. What constraints can be put on storage time in volcanic systems from purely thermodynamic considerations?

A volcanic system can be crudely modeled as a magma storage zone in the crust and a volcanic pile at the surface (Figure 4). Four processes affect the volume of magma in the storage reservoir or magma chamber: eruption ($Q_e$) and solidification ($Q_s$) remove magma from the system, while recharge ($Q_r$) and crustal assimilation ($Q_a$) add magma to the system. When a volcano acts as a closed system (one that receives no input of mass or heat via advected hot magma) all of the magma erupted remains molten for the duration of volcanic activity under consideration. In such a system, crystallization can occur due to the loss of heat or volatiles from the magma body to its colder surroundings but the extent of crystallization must
be insufficient to preclude eruption. One way to approach this problem is to assume that volcanoes act as closed systems during repose periods between eruptions and treat each eruption as the result an isolated batch of magma supplied by recharge in a single event and stored until eruption.

[27] Simple heat transfer considerations based on Stefan cooling of magma permit a first-order test of the hypothesis that a volcanic system is a closed system. If we know the eruption rate (Tables 1 and 2), and assume a closed system with respect to mass and heat recharge, the magma in storage will solidify at a rate specified by Stefan cooling. Using data for volcanic output rate of individual eruptions and repose time between eruptions gathered for several volcanic centers at a wide range of eruptive compositions, a simple 1-D Stefan cooling model [Carslaw and Jaeger, 1959] can be applied to estimate solidification times \( t \) (years) in a spherical magma volume of \( V \) (km\(^3\))

\[
t = \left( \frac{\sqrt{V}}{2 \kappa \sqrt{\lambda}} \right)^2,
\]

where \( \kappa \) is the thermal diffusivity, \( \lambda \) is the solution to the transcendental equation

\[
L \sqrt{\pi \frac{\Delta T}{c_p \lambda}} = \lambda^{-1} \text{erfc}(\lambda) e^{-\lambda^2},
\]

where \( L \) is the latent heat of fusion (J kg\(^{-1}\)), \( c_p \) is the isobaric specific heat capacity (J kg\(^{-1}\) K\(^{-1}\)), and \( \Delta T \) is the temperature difference between the ambient external temperature and the liquidus of the melt phase. The thermal diffusivity is calculated as

\[
\kappa = K \rho^{-1} c_p^{-1},
\]

where \( \rho \) is magma density (kg m\(^{-3}\)) and \( K \) is magma thermal conductivity (J/kg m s). Values for the various constants are taken from Spera [2000] for gabbro, granodiorite, and granite melts. This very basic approach permits a first-order look at the issue of cooling as a constraint on magma system longevity and openness. Heat calculations for lens or sill-like geometries alter the results by a factor of 2–4 [Fedotov, 1982]. Consideration of hydrothermal cooling would tend to enhance cooling rates so that the lifetime of a given volume of magma presented here is always an upper limit on cooling times. A more complex model is not justified given the order-of-magnitude estimates used as input.

[28] If we consider that volcanoes act as closed systems only between two successive eruptions, the solution to the 1-D Stefan Problem described above allows us to examine the thermal viability of the volcanic system given the repose period and the volume of magma involved (Figure 5). A closed system, in this context, means that one batch of magma is intruded at some time and stored until the eruption. Thus a maximum “storage time” for a batch of magma in the shallow plumbing system of a volcano can be estimated (Figure 6). The solidification time is determined as the time for a volume of magma to completely solidify as calculated from equation (1). The volume of magma is assumed to be five times the DRE volume of the eruption following the repose period based on the average I:E ratio from the data in Table 3. The assumption of complete solidification puts an upper limit on the time necessary to cool the magma enough to prevent eruption.

[29] Only a handful of volcanoes have been studied well enough to be able to estimate both volume and timing of eruptions over many eruptive cycles. The long, detailed records of eruptions at Mauna Loa [Klein, 1982] and Etna [Tanguy, 1979; Wadge, 1977] are used as examples of basaltic volcanoes, and the regular eruptive pattern at Izu-Oshima for the past 10\(^3\) years [Koyama and Hayakawa, 1996; Nakamura, 1964] makes the volumes of individual eruptions more clear. Toba [Chesner and Rose, 1991] and Yellowstone [Christiansen, 2001] are two calderas with a high quality record of multiple major eruptions. A few other examples from volcanoes with shorter, but still well-documented, records are also used with data from sources cited in Table 2.

[30] Whether the magma would solidify, and thus require the volcano to be an open system, depends on the magma storage time. Estimates of magma storage times from various crystal-age geochronometers are available at a range of volcanic centers and suggest that magma storage period, like repose, is a function of silica content of the magma [see Reid, 2003, and references therein]. Storage time from crystal ages for basaltic systems are generally longer or equal to repose, while storage times for andesites and rhyolite systems are slightly shorter than or equal to repose. On the basis of this information, we can draw a set of lines for different fractions of storage to repose time representing the limits for volcanoes that may be thermally closed systems between eruptions (Figure 6).
The repose time between eruptions at large calderas (Yellowstone, Long Valley, and Toba) can be more than 10 times greater than the storage time and the volcanoes are still required to be open systems in this analysis (Figure 6). The basaltic systems (Etna, Mauna Loa, and Oshima) are required to be open systems in this analysis only if magma is stored more than 10–100 times longer than the repose period (Figure 6). A few outliers for Etna with extremely short eruption reposes arguably may be the same eruption, but it is easy to see why these might be from “closed” systems on the timescales presented.

4.3. Heat Flux Associated With Magma Transport

Rates of magmatism may be translated into excess heat flows for specific magmatic provinces to obtain estimates of advected heat via magmatism at regional scales over magmatic province timescales. For mafic eruption rate \( Q_e \) and an I:E ratio of \( R \), the volumetric rate of magma flow into the crust is \( RQ_e \). The excess heat power \( H \) (J yr\(^{-1}\)) associated with magma transport from mantle to crust is

\[
H = R\rho Q_e \Delta T \left[ c_p + L / (T_{\text{liquidus}} - T_{\text{solidus}}) \right],
\]

where \( \Delta T \) is the temperature difference between the magma and local crust, \( L \) is the enthalpy of crystallization (250–400 kJ/kg dependent on magma composition), \( \rho \) is magma density, \( c_p \) is the isobaric heat capacity of the magma, and \( T_{\text{liquidus}} - T_{\text{solidus}} \) is the liquidus to solidus temperature interval.

As an example, consider the Skye subprovince of the British Tertiary Igneous Province (BTIP). For the estimated volume eruption rate of 2 \( \times \) \( 10^{-3} \) km\(^3\)/yr averaged over \( \sim 1600 \) km\(^2\) area of Skye, the average excess heat flow is \( \sim 3.5 \times 10^7 \) J/m\(^2\)/yr (1.1 W/m\(^2\)). This excess heat flux is more than an order of magnitude greater than the average terrestrial global heat flux 0.09 W m\(^{-2}\). These estimates are consistent with a crustal thickening rate of \( \sim 5 \) km/My and a background (re-
The regional heat flux of 10–15 times the global average during 60–53 Ma. We conclude that the volume flux of magma in the active years of this part of the BTIP focused heat flow about an order of magnitude above the background at the regional scale for C24 5 Ma. The regional energy/mass balance estimate appears consistent with inferences drawn from geochemical modeling that point to significant magma recharge during magmatic evolution at Skye [Fowler et al., 2004].

The excess heat power divided by the area affected by volcanism can be compared to the average terrestrial heat flux to the area. The heat power into the crust due to magmatism is therefore approximately 10^{17} J/yr for an overall average eruption rate taken from Table 1 of 10^{-2} km³/yr for ~1000 km² of arc or ridge and I:E ratio of 5. Thus typical values for the “average” magmatic system, 10^1 W/m², exceed the global terrestrial background value of 10^{-1} W/m² by two orders of magnitude.

5. Conclusions

The 170 long-term estimates of volcanic output rate compiled from literature references from 1962–2004 corroborate much of the previously published information about magmatic systems but also reveal a few surprises. Long-term volcanic rates are higher for basaltic volcanoes than andesitic and rhyolitic volcanoes taken as a group. Oceanic hot spots, arcs, and ridges have an average volcanic output rate of 10^{-2} km³/yr while continental arcs and hot spots have an average output rate of 10^{-3} km³/yr, implying that thinner crust/lithosphere is associated with higher volcanic rates on average but not systematically.

For the small number of volcanic systems where adequate data exist (Table 3), the I:E ratio is most commonly less than 10:1 with 2–3:1 being the most commonly occurring value, and a median value of 5:1. On the basis of the data compiled here, there is little indication that composition is strongly or systematically associated with I:E ratio. We conclude only that further work needs to be done on this important topic.

In contrast, composition and repose period between eruptions (end to next start) are strongly linked. We found that an exponential relationship between repose period and silica content of the magma provides a satisfactory fit to the data.
[38] Purely on the basis of thermal considerations, volcanic systems must be open to recharge of magma between individual eruptions, except for the most frequently erupting basaltic volcanoes. The fact that basaltic systems are indeed open magmatic systems can be demonstrated by other means [e.g., Davidson et al., 1988; Gamble et al., 1999; Hildreth et al., 1986].

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