Phase transition in MgSiO₃ perovskite in the earth’s lower mantle

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Abstract

A new polymorph of MgSiO₃ more stable than the Pbnm-perovskite phase has been identified by first-principles computations. It has the CaIrO₃ structure with Cmcm symmetry and consists of SiO₃ layers intercalated by eightfold-coordinated Mg ions. High-temperature calculations within the quasiharmonic approximation give a volume change of ~ 1.5% and a Clapeyron slope of ~ 7.5 ± 0.3 MPa/K at ~ 2750 K and ~ 125 GPa. These pressure–temperature (P–T) conditions are close to those in which a phase transition in MgSiO₃-perovskite has been observed by in situ angle dispersive X-ray diffraction measurements. This transition appears to be associated with the D" discontinuity.

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1. Introduction

The high-pressure Pbnm-perovskite polymorph of MgSiO₃ [1] is believed to be the most abundant mineral in the earth’s lower mantle [2]. The possibility of a phase transition in this polymorph has been controversial for several years. Reports of its dissociation into SiO₂ and MgO at 70–80 GPa and 3000 K [3,4], or of a possibly subtle phase change above 83 GPa and 1700 K [5], or of no phase transition at all [6] up to 94 GPa and 2500 K, have appeared in the literature. Although the pressure–temperature (P–T) conditions in these experiments were quite high, none of them had reached the conditions expected in the D" region. Recently, a drastic change in the X-ray diffraction of perovskite, suggesting a radical structural change, was observed at 125 GPa and 2500 K [7], and, more recently, the post-perovskite crystal structure was reported [8]. Understanding of the post-perovskite transition and of the properties of the post-perovskite phase is essential for a better understanding of the deep lower mantle, particularly of the D" region [9–13]. Here we show through first-principles high P–T computations that a structural transition occurs in Pbnm-perovskite.

2. The post-perovskite structure

The techniques used here and the details of this calculation are similar to those used in previous high P–T calculations of the Pbnm-perovskite phase [14].
Computations were performed using the local density approximated (LDA) [15,16] and the generalized gradient approximation (GGA) [17]. Pseudopotentials for oxygen and silicon were generated by the methods of Troullier and Martins [18]. The cutoff radii are: (a) for oxygen in the configuration 2s² 2p⁴, \( r(2s) = r(2p) = 1.45 \) a.u., with p nonlocality; (b) for silicon in the configuration 3s² 3p⁴ 3d⁰, \( r(3s) = 1.47 \) a.u., \( r(3p) = 1.47 \) a.u., \( r(3d) = 1.47 \) a.u., with d nonlocality. The method of von Barth and Car [19] was used for magnesium. Five configurations, 3s² 3p⁰, 3s¹ 3p¹, 3s¹ 3p⁰ 3d⁰, 3s¹ 3p⁰ 0.5 3d⁰ 0.5, 3s¹ 3p⁰ 0.5 3s¹ 3d¹ with decreasing weights 1.5, 0.6, 0.3, 0.3, and 0.2, respectively, were used. Cutoff radii were \( r(3s) = 2.5 \) a.u. with d nonlocality. The plane wave energy cutoff was 70 Ry. Brillouin zone sampling for electronic states (phonons) was carried out on 6 (14) and 2 special (18) k-points (q-points) for the perovskite and post-perovskite phases, respectively. Phonon frequencies were obtained using density functional perturbation theory [20,21]. Structural searches were performed using variable cell shape molecular dynamics [22]. Thermodynamic properties were determined using the quasiharmonic approximation [23]. Computations were performed with the PWscf code [24].

The search for the post-perovskite structure was guided by two general principles: (a) polyhedron
types and interconnections that would be reasonable at ultrahigh pressures; and (b) extrapolation of the compressive mechanism of the Pbnm-perovskite structure. Edge-sharing rutile-like columns form a more compact octahedral arrangement, but the stoichiometry requires these columns to be connected by the octahedral apices. This produces the SiO$_3$ layers. These layers should then be intercalated by magnesium ions with the highest possible coordination. These criteria produce a family of structures. After exploring more than 30 prototypes, we found, independently, this one shown in Fig. 1. All attempted structures were fully optimized above 120 GPa using variable cell shape damped molecular dynamics [22], and their enthalpies were then compared with Pbnm-perovskite’s. The structure in Fig. 1 is the only one we found with lower enthalpy than perovskite in static LDA [15,16] and/or generalized gradient approximation (GGA) [17] calculations. This is the structure of CaIrO$_3$ [25], the same one found by Murakami et al. [8]. This structure is base-centered orthorhombic with space group Cmcm. Magnesium ions are located in approximately eightfold-coordinated sites, at the center of irregular hendecahedra. Like the Pbnm-perovskite structure, it has four formulae unit per conventional cell ($Z = 4$), but it is very anisotropic. Static isotropic compression using LDA revealed a transition pressure of 98 ± 3 GPa (109 ± 4 GPa using the GGA).

The relationship between this Cmcm and the Pbnm structures can be understood on the basis of the extrapolated compressive behavior of MgSiO$_3$-perovskite [26]. The angles between the octahedral edges bisected by the (110) plane in the Pbnm structure (see Fig. 2) decrease faster than other similar angles. The Cmcm structure can be produced by forcing these angles to close faster under strain $\varepsilon_6$. Fig. 2 shows structures that result by applying strains $\varepsilon_6$ in the Pbnm-perovskite first equilibrated at 120 GPa. For sufficiently large strains, these angles vanish and form edge-sharing rutile columns when one of the oxygens in each pair of edges defining these angles is removed. This process forces layer formation. In the third direction, perpendicular to the columns and to the layers, octahedra remain connected at the apices. According to this transition mechanism, the [100]$_{ppv}$, [010]$_{ppv}$, and [001]$_{ppv}$ directions in the Cmcm structure correspond to the [110]$_{ppv}$, [110]$_{ppv}$, and [001]$_{ppv}$ in the Pbnm structure, respectively. Structural parameters obtained in static LDA calculations at 120 GPa are given in

Fig. 2. Relaxed (optimized) Pbnm-perovskite structure at 120 GPa under shear strain $\varepsilon_6$. Following the relaxation of internal degrees of freedom with $\varepsilon_6 = 0.4$, a complete relaxation was performed.
Table 1. The inset in Fig. 4B shows the pressure dependence of the $b/a$ and $c/a$ ratios in this phase as obtained from static calculations. As expected, the structure is more compressible along [010].

3. Thermodynamic properties and phase equilibrium

We then proceeded with calculations of phonon dispersions and vibrational densities of states (VDOS) (see Fig. 3) to obtain Gibbs free energies within the QHA. Finite temperature equation of state (EoS) parameters is also summarized in Table 1. The uncertainties in these parameters represent the range of values obtained by fitting third-order finite strain and Vinet et al. [27] EoSs. The Debye temperature was estimated by fitting the specific heat to the Debye model. Values for perovskite are in parentheses.
Fig. 4. (A) Helmholtz free energy versus volume at various temperatures for perovskite (blue) and post-perovskite (red) and (B) calculated compression curves of perovskite (blue) and post-perovskite (red). Dashed lines in (B) correspond to conditions where the validity of the QHA is questionable.
underestimate bulk moduli, with deviations being smaller with the former (see [14] and references therein). However, there is little experience with the effect of these systematic deviations and with the use of the QHA on calculated transition pressures. A recent detailed LDA calculation of the akimotoite-to-perovskite transition in MgSiO$_3$ [28] indicated that transition pressures with LDA are underestimated by $\sim$ 5 GPa and the Clapeyron, negative one in that case, is overestimated. The main source of these deviations is the description of the exchange correlation energy in density functional theory. In static calculations, LDA tends to underestimate transition pressures and GGA results are usually in better agreement with experiments. The inclusion of zero-point motion in the calculation of a phase boundary with positive Clapeyron slope shifts the boundary to higher pressures [28], $\sim$ 2 GPa in this case. It is therefore reasonable to anticipate that the true transition pressure falls between the phase boundaries given by LDA and GGA. Direct comparison of the Gibbs free energies of both phases produces the phase boundary shown in Fig. 5. The width represents the range of values obtained using the LDA (left bound) and the GGA (right bound). Intermediate values for the transition pressures are expected to be more realistic. Indeed, these values are closer to Murakami’s estimation of the phase boundary position [7,8]. However, there are also large uncertainties associated with the platinum scale in this $P$–$T$ range [29,30]. It tends to overestimate pressure by $\sim$ 10 GPa when compared with the gold scale [31]. The Clapeyron slope at 2500 K is $\sim$ 7.5 $\pm$ 0.3 MPa/K.

4. Geophysical significance

This transition is important for understanding the state of the deep lower mantle, particularly that of the D$''$ region, at the bottom 300 km [9–13]. The D$''$ layer has wide topography [10] and is quite anisotropic [12]. Chemical heterogeneity, partial melting, phase transitions, preferred orientations, or a combination of all of these have been proposed as possible mineralogical origins of these features. In particular, it has been argued on the basis of seismic and geodynamic considerations that a solid–solid phase changes with a Clapeyron slope of $\sim$ 6 MPa/K [9] could cause the observed topography. Our Clapeyron slope of 7.5 $\pm$ 0.3 MPa/K is quite close to this value. The presence of alloying elements, such as aluminum and iron, is likely to affect the transition pressure and the Clapeyron slope, particularly if minor element partitioning between MgSiO$_3$ and other coexisting phases is affected. For instance, silicon and magnesium polyhedral volumes increase and decrease, respectively, across the transformation (see Table 1). This might affect element partitioning. It suggests also that aluminum- or aluminum- and iron-(III)-bearing perovskite [perovskite with coupled (Al$^{3+}$, Al$^{3+}$) or (Al$^{3+}$, Fe$^{3+}$) substitution for (Mg, Si)] should transform at lower pressures, while iron-(II)-bearing perovskite (Fe$^{2+}$ substitution for Mg$^{2+}$) might transform at higher pressures, maybe accompanied by a high- to low-spin transition in iron, as happens in ferroperriclase [32] (Fe$^{2+}$ is “larger” in the high-spin state configuration). The structural relationship between the $P$bnm and the $Cmcm$ phases found here suggests that also shear stresses are likely to affect the transition pressure (in both directions). Shear stresses are expected particularly near the CMB. Also, the possibility of an intervening perovskite phase with different symmetry as suggested by Shim et al. [5], could increase the post-perovskite transition pressure.

Across the D$''$ topography, pressure varies from $\sim$ 125 to $\sim$ 133 GPa. This is indicated in Fig. 5 by the vertical semitransparent gray band. Our best estimate of the transition temperature in pure MgSiO$_3$-perovskite through this pressure range is 2750–3800 $\pm$ 250 K. These temperatures are consistent with the existence of a post-perovskite transition before the core–mantle boundary where temperatures can reach $\sim$ 4100 K [33,34] and point to the possibility of 1000 K lateral temperature variations in this region. However, the effect of composition, stress state, and of a possible intervening perovskite structure [5] on this transition still must be investigated before an attempt is made to relate the D$''$ topography and lateral temperature variations through the post-perovskite transition.

The layered post-perovskite structure is potentially very anisotropic. Although reaction products between molten iron and MgSiO$_3$, such as FeSi, FeO, SiO$_2$, and FeO, are anticipated to co-exist in this region, in addition to an accumulation of light elements from the core, MgSiO$_3$-post-perovskite might be the most abundant phase in D$''$, and preferred orientation in
this structure is an additional potential source of anisotropy in this region.

5. Conclusion

A new polymorph of MgSiO$_3$ with the CaIrO$_3$ structure and more stable than the $Pbnm$-perovskite phase has been identified by first-principles computations. The CaIrO$_3$ structure is shown to be related with the $Pbnm$-perovskite structure through a shear strain $\varepsilon_6$. This structural relationship suggests that the post-perovskite phase transition pressure might be affected by shear stresses. Quasiharmonic high-temperature calculations of the thermodynamic phase boundary gives a Clapeyron slope of $\sim 7.5 \pm 0.3$ MPa/K at $\sim 2750$ K and $\sim 125$ GPa. These $P$--$T$ conditions are close to those anticipated in the D'' region and this Clapeyron slope is close to that anticipated if the D'' topography were related to a solid–solid transformation. Our results suggest that the post-perovskite transition might be associated with the D'' discontinuity and that this layered polymorph might provide an additional source of anisotropy in the D'' region.

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